# Prospects for Galactic and stellar astrophysics with asteroseismology of giant stars in the *TESS* Continuous Viewing Zones and beyond

J. Ted Mackereth<sup>1,2,3</sup>\*<sup>†</sup>, Andrea Miglio<sup>1</sup>, Yvonne Elsworth<sup>1</sup>, Benoit Mosser<sup>4</sup>, Savita Mathur<sup>5,6</sup>, Rafael A. Garcia<sup>7,8</sup>, Domenico Nardiello<sup>9,10</sup>, Oliver J. Hall<sup>1</sup>, Mathieu Vrard<sup>11</sup>, Warrick H. Ball<sup>1</sup>, Sarbani Basu<sup>12</sup>, Rachael L. Beaton<sup>13,14</sup>‡<sup>§</sup>, Paul G. Beck<sup>15,5</sup>, Maria Bergemann<sup>16</sup>, Diego Bossini<sup>17</sup>, Luca Casagrande<sup>18</sup>, Tiago L. Campante<sup>17,19</sup>, William J. Chaplin<sup>1</sup>, Cristina Chiappini<sup>20</sup>, Léo Girardi<sup>10</sup>, Andreas Christ Sølvsten Jørgensen<sup>1</sup>, Saniya Khan<sup>1</sup>, Josefina Montalbán<sup>1</sup>, Martin B. Nielsen<sup>1</sup>, Marc H. Pinsonneault<sup>21</sup>, Thaíse S. Rodrigues<sup>10</sup>, Aldo Serenelli<sup>22,23</sup>, Victor Silva Aguirre<sup>24</sup>, Dennis Stello<sup>25</sup>, Jamie Tayar<sup>26</sup><sup>†</sup>, Johanna Teske<sup>27,28</sup><sup>†</sup>, Jennifer L. Van Saders<sup>26</sup> and Emma Willett<sup>1</sup>

# ABSTRACT

The NASA-TESS mission presents a treasure trove for understanding the stars it observes and the Milky Way, in which they reside. We present a first look at the prospects for Galactic and stellar astrophysics by performing initial asteroseismic analyses of bright (G < 11) red giant stars in the TESS Southern Continuous Viewing Zone (SCVZ). Using three independent pipelines, we detect  $v_{\text{max}}$  and  $\Delta v$  in 41% of the 15,405 star parent sample (6,388 stars), with consistency at a level of ~ 2% in  $v_{\text{max}}$  and ~ 5% in  $\Delta v$ . Based on this, we predict that seismology will be attainable for ~ 3 × 10<sup>5</sup> giants across the whole sky and at least 10<sup>4</sup> giants with  $\geq$  1 year of observations in the *TESS*-CVZs, subject to improvements in analysis and data reduction techniques. The best quality TESS-CVZ data, for 5,574 stars where pipelines returned consistent results, provide high quality power spectra across a number of stellar evolutionary states. This makes possible studies of, for example, the Asymptotic Giant Branch bump (AGBb). Furthermore, we demonstrate that mixed  $\ell = 1$  modes and rotational splitting are cleanly observed in the 1-year data set. By combining TESS-CVZ data with TESS-HERMES, SkyMapper, APOGEE and Gaia we demonstrate its strong potential for Galactic archaeology studies, providing good age precision and accuracy that reproduces well the age of high  $\left[\alpha/\text{Fe}\right]$  stars and relationships between mass and kinematics from previous studies based on e.g. Kepler. Better quality astrometry and simpler target selection than the Kepler sample makes this data ideal for studies of the local star formation history and evolution of the Galactic disc. These results provide a strong case for detailed spectroscopic follow-up in the CVZs to complement that which has been (or will be) collected by current surveys.

**Key words:** stars: fundamental parameters – stars: oscillations – Galaxy: fundamental parameters – Galaxy: structure – Galaxy: kinematics and dynamics – Galaxy: stellar content

#### \* E-mail: tedmackereth@cita.utoronto.com

† NSERC Banting Fellow

‡ NASA Hubble Fellow § Carnegie-Princeton Fellow

§ Carnegie-Trinecton Tenow

# **1 INTRODUCTION**

Asteroseismology, the study of stellar oscillations, made possible through space based, long duration photometry of stars in missions such as CoRoT (Baglin et al. 2006; Auvergne et al. 2009), *Kepler* (Borucki et al. 2010) and K2 (Howell et al. 2014) has brought about a paradigm shift in our understanding of stellar structure and evo-

lution. Our improved understanding of stellar interiors, driven by these missions, has led in-turn to a step-change in precision on the estimates of stellar parameters such as mass, radius and age that can be ascertained from our analysis of observed oscillations and their comparison with detailed stellar modelling. In turn, asteroseismology provides an ideal means by which to improve and constrain such stellar models (for reviews, see, e.g. Chaplin & Miglio 2013; Aerts 2019).

Stellar ages are an important aspect of the endeavour toward understanding the formation and evolution of the Milky Way, providing all important chronological context to these studies. Asteroseismic ages have already proven extremely useful in understanding aspects of the formation and evolution of the Milky Way disc (Anders et al. 2017b; Silva Aguirre et al. 2018; Miglio et al. 2020) and more recently, the halo (Chaplin et al. 2020; Montalbán et al. 2020). Combining asteroseismic constraints with other observational methods, such as near infra-red (NIR) spectroscopy (e.g. the APOKASC catalogue: Pinsonneault et al. 2014, 2018), have allowed for the extrapolation of asteroseismic ages onto larger samples of stars for which seismic data is not available (Martig et al. 2016; Ness et al. 2016; Ting & Rix 2018; Das & Sanders 2019; Mackereth et al. 2019). Extending the sample size and better measuring and understanding the stars in these vital training data will no doubt play a key role in the future of asteroseismology-driven Galactic studies. Such multi-dimensional data sets, observed by multiple surveys, also provide an ideal means by which to calibrate data between surveys.

The NASA Transiting Exoplanet Survey Satellite (TESS) mission (Ricker et al. 2015) was designed with a focus on the detection of nearby exoplanets (e.g. Sullivan et al. 2015). However, at the end of its 'prime' 2-year mission, it will have provided time series photometry of stars on an all-sky basis in both targeted, short cadence data and wide field 30-minute cadence Full Frame Images (FFI)<sup>1</sup>. This will increase the number of stars with detectable asteroseismic oscillations by at least an order of magnitude over Kepler and CoRoT (e.g. Thomas et al. 2017; Schofield et al. 2019; Silva Aguirre et al. 2020). Indeed, the asteroseismic potential of TESS has already been explored using early data products (e.g. Huber et al. 2019; Campante et al. 2019; Chaplin et al. 2020). The first two years of TESS all-sky observations were taken in 27 day sectors that overlap at the ecliptic poles, forming what is referred to as the continuous viewing zones (CVZ), within which a complete year of continuous data has now been gathered. Stars in the CVZs are likely to have power spectra that better sample lower frequency signals than those with single sectors of data. The data for these stars can be analysed in greater detail, offering higher fidelity insights into their interiors and generating more precise estimates of their parameters.

In this paper, we present a first look at the asteroseismic constraints which are possible for stars in the *TESS*-SCVZ, based on the publicly released full frame images (FFI) of the first year of *TESS* data. The SCVZ data has been fully available for over a year, providing ample time for detailed reduction of its time-series data. By selecting a sample of very bright (G < 11) giant stars based on *Gaia* DR2 (Gaia Collaboration et al. 2018) and 2MASS (Skrutskie et al. 2006) photometry, we demonstrate that the detection of stellar oscillations in the CVZ data across many evolutionary stages on the giant branch will allow detailed studies of stellar structure and evolution. This data will facilitate studies of the nearby Galactic stellar populations in age space, providing a strong justification for the necessity of gathering extended spectroscopic data for such samples.

In Section 2, we present the *TESS*-SCVZ bright giant sample, outlining the sample selection criteria and photometry of the FFI as well as presenting the external spectroscopic, photometric and kinematic constraints that we use to study the properties of the sample. Section 3 presents the results of our asteroseismic analyses. There, we discuss the seismic detection yields before showing the potential of these data for stellar and Galactic astrophysics. Finally, in Section 4 we summarise our findings and make conclusions on the potential of the data-set and the extrapolation of these results to the all-sky sample.

#### 2 THE TESS-SCVZ BRIGHT GIANT SAMPLE

We first describe the compilation of a catalogue of stars in and around the *TESS* southern continuous viewing zone for which we aim to achieve asteroseismic constraints. To this end, we select targets from *Gaia* and 2MASS, whose photometry is then extracted from the *TESS* full frame images (FFI) and processed to asteroseismic power spectra. These spectra are then analysed by three independent pipelines to establish the global seismic parameters  $v_{max}$  and  $\Delta v$ . We complement this data with spectroscopic constraints which include the necessary stellar parameters to establish estimates of the stellar mass (and therefore age) using the Bayesian tool PARAM (described below). Furthermore, we include kinematic constraints which allow the inspection of this data in full six-dimensional phase space. The data set is described below, and the resulting catalogue (available online) in Appendix D.

#### 2.1 The parent sample: Gaia and 2MASS data

We compile a target list of stars in and near to the southern CVZ (SCVZ), for which TESS observations are now complete, by making a cone-search from Gaia DR2 (Gaia Collaboration et al. 2018) within 20° of the southern ecliptic pole. We cross match this set with 2MASS (Skrutskie et al. 2006) and select stars with G < 11and parallax signal-to-noise  $\pi/\delta \sigma > 20$  (i.e. uncertainties of < 5%), isolating the brightest targets with the most precise parallax measurements, for which we expect the greatest yield of asteroseismic parameters. Because we select the brightest and therefore nearby stars, we are likely unaffected by the population effects from parallax SNR selection discussed by Luri et al. (2018). We then select stars with  $(J - K_S) > 0.5$  and  $M_H < 3$  (estimating  $M_H$  using only the inverted parallax and ignoring the effects of extinction although we do account for this later), isolating a final sample of 15,405 giant stars including 3,019 with at least 12 sectors (27-day chunks) of data. The 'true' CVZ is within  $\sim 10^\circ$  of the ecliptic pole, so this sample includes 12,386 stars that have less than 12 sectors of data. The data in this region of the sky therefore has a wide range in dwell time and observing pattern, making it ideal for tests of data products and yields all-sky. The on-sky distribution of the stars in the input catalogue is shown in polar projection in Figure 1. The number of sectors for which photometry was recovered is indicated by the colour of the points, demonstrating the geometric effects imposed on the data by the pointing scheme of TESS. Inside the CVZ, there are a number of stars with less than optimal length time-series. Furthermore, the sample is clearly biased to be nearby, such that 95% of targets have inverse parallaxes of

<sup>&</sup>lt;sup>1</sup> The FFI will be re-observed in the extended mission, at 10-minute cadence, in the second half of 2020.



**Figure 1.** The *TESS*-SCVZ bright giant G < 11 sample in polar projection, demonstrating how the number of available sectors changes with position on sky, due to the *TESS* pointing scheme. Each camera has a  $24^{\circ} \times 24^{\circ}$  field-of-view, providing a ~  $24^{\circ}$  circular zone with many stars with 13 sectors of continuous observations. In this bright sample, many geometric selection effects are visible, due mainly to gaps in the camera CCDs.

d < 1.7 kpc. Importantly, geometric and distance selection effects may be necessary to account for in future studies which require forward modelling.

# 2.2 Extraction of light curves from the TESS FFI

We extract photometry from the *TESS* Full Frame Images (FFI) for all 15,405 stars in the target list, following the methods presented in Nardiello et al. (2019). Briefly, this method models the *TESS* PSF, accounting for spatial and temporal variations to perform photometry and neighbour subtraction (for sources between 10" and 400" from the target star) where fields are crowded. We extract light curves from the FFI using the img21c code presented in Nardiello et al. (2015, 2016). The pipeline corrects for some systematic effects associated with the spacecraft, detector, and environment by modelling them using the co-trending basis vectors (CBVs) obtained by Nardiello et al. (2020). As an example, this allows for reconstruction of the light curves where a pointing problem caused a systematic loss of flux in sector 1.

The resulting light curves are then post-processed using methods outlined in García et al. (2011). Gaps in the light curves which are larger than 3 sectors (~ 81 days) are removed by a comparison of the gap length and lifetime of any modes observed in the data, while smaller gaps are in-painted. This also removes artefacts in the data resulting from outlying data points due to target drift at the start of sectors (e.g. as the spacecraft finalised its positioning). Finally, a high-pass filter at 2 days (~ 5  $\mu$ Hz) is applied to the time-series to remove any long term trends (this affects the detection of oscillations lower than  $\nu \sim 10 \mu$ Hz). These light curves are then transformed into power spectra in frequency space using a Lomb-Scargle periodogram estimate with an oversampling factor of 10.

The power spectra are analysed by three pipelines to determine the global parameters  $v_{max}$ , the frequency at maximum power, and  $\Delta v$ , the mean spacing between pressure modes of the same degree *l* at successive radial orders. The pipelines in question are presented in Mosser & Appourchaux (2009), Elsworth et al. (2020) and Mathur et al. (2010); we refer to them here as COR, BHM and A2Z, respectively (similarly to, e.g. Pinsonneault et al. 2018). COR and A2Z use the power spectra for analysis while BHM uses directly the time-series data. All the pipelines use independent approaches to determine the parameters, providing a means by which to assess the internal consistency in the results.

#### 2.3 Spectroscopic and photometric parameters

In order to robustly determine useful stellar parameters such as mass and radius using the global seismic parameters, independent measures of the stellar effective temperature  $T_{\rm eff}$  and optionally, as additional constraints, surface gravities log(g) and/or metallicity Z, are necessary. In the case of the TESS-SCVZ, there is little publicly available spectroscopic data from which to derive these quantities (as of the preparation of this manuscript). We demonstrate below that the gathering of detailed spectroscopy for these targets will be of great utility for the community. However, for the purposes of this 'proof-of-concept' study, we combine constraints on these quantities from the catalog of  $T_{\text{eff}}$  and [Fe/H] derived in Casagrande et al. (2019) from the SkyMapper photometric survey DR1.1 (Wolf et al. 2018) with the TESS-HERMES DR1 data (Sharma et al. 2018), which provides spectroscopic constraints on  $\log(g)$  (but not yet on  $T_{\rm eff}$  or [Fe/H] for these bright giants). In total, we find that only 1186 of the 15405 giants have all three parameters available in these catalogues. By requiring a constraint only on  $T_{\rm eff}$  (e.g. as required when deriving the mass and radii from the asteroseismic scaling relations: Kjeldsen & Bedding 1995) the sample size increases to 8249 stars. For the stars without spectroscopic log(g)from *TESS*-HERMES, we infer a posterior on log(g) using the sample with full spectro-photometric information as a training set using the methodology described in Appendix A.

We also make use of the SDSS-IV/APOGEE-2 DR16 (Majewski et al. 2017; Ahumada et al. 2019) spectroscopic catalogue of southern stars to perform a cross check of parameters derived using SkyMapper and TESS-HERMES stellar parameters. APOGEE also includes detailed element abundance information derived through the application of APOGEE Stellar Parameters and Chemical Abundances Pipeline (ASPCAP: García Pérez et al. 2016) - which uses a specifically derived linelist (Shetrone et al. 2015) - to spectra of the NIR H-band taken using the twin (Southern) APOGEE spectrograph (Wilson et al. 2019) on the 2.5m Irénée du Pont telescope at Las Cumbres Observatory (LCO: Bowen & Vaughan 1973). APOGEE spectra are then reduced and analysed using in-house pipelines (Nidever et al. 2015; Jönsson et al. 2020). Red giants in the TESS-CVZs are specifically targeted within APOGEE via external program time through the Carnegie Institution of Science (PIs: Beaton, van Saders, and Teske). Information about these extra targets and more generally about APOGEE-2 targeting is presented in Beaton et al. (2020, in prep.) and Santana et al. (2020, in prep.). Using the APOGEE abundances, we can make some initial insights into the connections between stellar age and element abundances

in the Galaxy. We find that APOGEE-2 DR16 has 513 targets in common with our bright *TESS*-CVZ giants. The SkyMapper  $T_{\rm eff}$  and [Fe/H] generally agree well (within  $1\sigma$ ) with those derived by APOGEE, in the cases where both surveys returned these parameters.

We use these spectroscopic and photometric stellar parameters to determine bolometric corrections in the J, H and  $K_S$  band for each of the targets represented in all the relevant data sets. We use the bolometric-corrections code<sup>2</sup>, which applies methods described in Casagrande & VandenBerg (2014). We then use this correction, in conjunction with the Gaia DR2 parallax information and the 2MASS photometry to determine the luminosity of each of the targets. The  $K_S$  band extinction  $A_{K_S}$  is determined for each target using the Combined19 dustmap (built from the combined dustmaps of Drimmel et al. 2003; Marshall et al. 2006; Green et al. 2019) implemented in the mwdust<sup>3</sup> Python package (Bovy et al. 2016). We transform  $A_{K_S}$  for the J and H band using the ratios determined by Indebetouw et al. (2005). We calculate the uncertainty on the luminosity by propagating those on  $T_{\text{eff}}$ ,  $\log(g)$  and [Fe/H] into the bolometric correction. Parallax uncertainties are propagated when computing absolute magnitudes. We compare the photometric luminosity with that determined from seismic parameters and scaling relations in Appendix C, and discuss this in relation to systematics in TESS in Section 3.1.

The parameters are then used, in conjunction with the pipeline constraints on  $v_{max}$  and  $\Delta v$ , to determine mass, radius and age estimates for the sample via a Bayesian comparison with stellar models using the PARAM code (da Silva et al. 2006; Rodrigues et al. 2014, 2017). We generate results separately based on the *SkyMapper/TESS*-HERMES and APOGEE DR16 parameters, including both in our catalogue. PARAM provides full posterior information on age and mass based on the input observables (and their uncertainties). We report here and in the catalogue the median and interquartile range of the posterior distributions as our final mass, radius and age constraints.

While PARAM provides a robust way to estimate mass and age based on the seismic and spectro-photometric constraints, it has a number of important caveats. Of course, any comparison to stellar models is subject to the limitations of the model predictions themselves. Similarly, the comparison between models and data is hampered by details such as the so-called surface effects which are not currently modelled and likely depend on stellar parameters in complex ways (e.g. Manchon et al. 2018). However, a number of tests have shown that this method provides accurate mass estimates to within a few per-cent when compared to eclipsing binaries and clusters (e.g. Miglio et al. 2016; Rodrigues et al. 2017; Handberg et al. 2017; Brogaard et al. 2018). The PARAM approach also avoids the usual problems in understanding uncertainties associated with corrections to the  $\Delta v$  scaling relation (e.g. Brogaard et al. 2018).

#### 2.4 Stellar kinematic constraints

We obtain kinematic constraints for the sample using astrometric parameters from the *Gaia* DR2 (Gaia Collaboration et al. 2018) catalogue. The proper motion  $\mu_{[l,b]}$  and radial velocity  $v_{helio}$  constraints provided by *Gaia* in this bright and nearby regime are likely to be accurate, and so we apply these without correction or adjustment for zero-point offsets or biases, which are small in compar-

ison to parameter values. The more important parallax zero-point offsets in the (now extensive) literature (e.g. Lindegren et al. 2018; Schönrich et al. 2019; Khan et al. 2019; Hall et al. 2019; Leung & Bovy 2019; Zinn et al. 2019; Chan & Bovy 2020) range from  $30 \leq \Delta \omega \leq 60 \mu as$ , agreeing that the raw *Gaia* DR2 values are too small. The majority of these groups consistently find an offset in the region of 50  $\mu as$ . We make a simplified assessment of the parallax zero-point offset implied by our seismic results in Appendix B, finding an offset of  $30 \pm 2 \mu as$  for this nearby, bright sample, which we apply externally to every star in our catalogue. This implies a  $\leq 3\%$  decrease in distance to the majority of the stars we consider. We defer a more detailed assessment of the *Gaia* parallax zero-point offset using *TESS* to future studies.

To propagate astrometric parameters to Galactocentric coordinates, we take 100 samples of the joint posterior of the parameters using the median, uncertainty and correlation coefficients for each. Throughout the paper, we adopt a solar position of  $[R_{\odot}, z_{\odot}] = [8.125, 0.02]$  kpc (Gravity Collaboration et al. 2018; Bennett & Bovy 2018) and a corresponding velocity  $\vec{v}_{\odot} = [U, V, W] = [-11.1, 245.6, 7.25]$  km s<sup>-1</sup> based on the combined constraints of Schönrich et al. (2010) and the SGR A\* proper motion from Gravity Collaboration et al. (2018). We process every sample of the astrometric parameters into the left-handed Galactocentric cylindrical coordinate frame. The resulting uncertainties on  $v_R$ ,  $v_T$  and  $v_z$  are  $\sim 1 \text{ km s}^1$ .

Finally, we estimate the orbital parameters  $r_{peri}$ ,  $r_{apo}$ , e and  $z_{max}$  for each sample of each stars phase space coordinates using the fast orbit estimation method described by Mackereth & Bovy (2018) and implemented in galpy (Bovy 2015), adopting the simple MWPotential2014 potential included there. We include these estimations in our final catalogue, reporting the median and interquartile range of the resulting posterior distribution of orbital parameters for each star. The median uncertainties on the final orbital parameters are less than 2%.

#### **3 RESULTS**

#### 3.1 Systematics in light curves derived from the FFI

Before looking in detail at our seismic results, we remove spurious seismic detections by comparing the luminosities computed based on the seismic parameters with those from *Gaia*. Stars that are erroneously assigned a low (high)  $\nu_{max}$  by any pipeline should have brighter (fainter) seismic luminosities relative to those derived directly from photometry, and so can be removed from further analysis. We perform this check by computing a 'seismic' luminosity  $L_{seis.}$ , via the asteroseismic scaling relation for the stellar radius R,

$$\left(\frac{R}{R_{\odot}}\right) \simeq \left(\frac{\nu_{\max}}{\nu_{\max_{\odot}}}\right) \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-2} \sqrt{\frac{T_{\text{eff}}}{T_{\text{eff}_{\odot}}}}$$
(1)

which can then be substituted into the relationship between the luminosity and radius:

$$\left(\frac{L}{L_{\odot}}\right) \simeq \left(\frac{R}{R_{\odot}}\right)^{2} \left(\frac{T_{\rm eff}}{T_{\rm eff_{\odot}}}\right)^{4} \tag{2}$$

achieving a relationship between luminosity and the global seismic parameters

$$\left(\frac{L}{L_{\odot}}\right) \simeq \left(\frac{\nu_{\max}}{\nu_{\max_{\odot}}}\right)^2 \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-4} \left(\frac{T_{\text{eff}}}{T_{\text{eff}_{\odot}}}\right)^5.$$
(3)

For each target where a photometric luminosity  $L_{phot}$  could be estimated using the spectrophotometric parameters, we take samples of

<sup>2</sup> https://github.com/casaluca/bolometric-corrections

<sup>&</sup>lt;sup>3</sup> https://github.com/jobovy/mwdust

the asteroseismic parameters and  $T_{\rm eff}$  assuming uncorrelated Gaussian uncertainties. We then propagate these samples through the above relationship to attain  $L_{\rm seis.}$  and it's associated uncertainty. Clearly, the precision and accuracy of  $L_{\rm seis.}$  can be improved beyond that achievable with scaling relationships (e.g. Khan et al. 2019), but this methodology is sufficiently accurate to detect false-positives.

We demonstrate the full comparison for each pipeline in Appendix C, but briefly summarise the results here. Between  $\sim 5$ to 15% of targets have a seismic luminosity which is more than  $3\sigma_c$  (where  $\sigma_c$  is defined at the uncertainties on each measurement added in quadrature) from the photometric value. The majority of problematic cases occur in bright stars, where pipelines return erroneously high  $v_{max}$  measurements. This is expected, since the frequency resolution of TESS is limited, making characterisation of the power spectrum more difficult at low frequencies (i.e.  $\nu \leq 10 \ \mu$ Hz). As an example, for 13 sectors of data, at a  $v_{\rm max} \sim 1 \ \mu {\rm Hz}$  the number of independent frequency bins in the spectrum around the power envelope is  $\sim 20$ . It should also be noted that the high-pass filtering applied to the light curves will strongly affect any possibility of detection below  $\sim 10 \ \mu\text{Hz}$ . We flag targets with  $|(L_{\text{phot.}} - L_{\text{seis.}})/\sigma_c| > 3$  for each pipeline in our final catalogue. Such discrepancies may also be explained by unresolved binary systems (Miglio et al. 2014), which have a higher than expected apparent luminosity, while the seismology represents usually just one component of the binary. The detection of such systems requires highly precise parallax measurements, such as those for these nearby targets, which have hitherto been unavailable to seismic samples (e.g. those from Kepler). Similarly, we expect that there should be a large presence of wide binary systems within this sample (such as those found in Kepler, e.g. Godoy-Rivera & Chanamé 2018), which can be useful for calibrating independent age measurement techniques (e.g. Chanamé & Ramírez 2012).

A number of targets also have apparently spurious detections at the diurnal frequency,  $v_{max} \approx 11.57 \ \mu$ Hz. We note that while many of these detections are consistent with that expected based on their photometric luminosities, at least some appear to be due to some spurious power excess at roughly this frequency. Extraction of the background signal from the FFI does appear to show such an excess, suggesting that this is due to some still existent issue with e.g. scattered light (such issues are noted in the *TESS* Data Release notes, Fausnaugh et al. 2018). To maximise the value of these data for asteroseismology, these systematics must be studied further and accounted for. Detailed analysis and correction for this is beyond the scope of this exploratory paper, and we simply remove problematic cases from our analysis.

#### 3.2 Detection yields and seismic constraints

We first examine the yield of seismic detections for the bright SCVZ red giants in all three pipelines and determine the sample where all analyses provided consistent results for the global parameters. We compare realised yields with simple predictions, computed using the formalism presented in Chaplin et al. (2011) and updated for *TESS* targets by Campante et al. (2016); Schofield et al. (2019), implemented for this sample as the asteroestimate<sup>4</sup> Python package. The model uses *Gaia* and 2MASS photometry, the *Gaia* parallax and time series length as input, but requires an



**Figure 2.**  $M_{K_S}$ - $(J - K_S)$  of the *TESS*-SCVZ bright giant sample. The contours demonstrate the regions in this space that contain 90% of the detections made by each of the pipelines (confirmed using photometric luminosities) and a model for the detection yield based on Chaplin et al. (2011) and Schofield et al. (2019) (described further in the text). The boundaries where  $v_{\text{max}}$  is equal to 10 and 280 µHz for a 1.1 M<sub>☉</sub> star. 10 µHz is likely the limit at which our light curve processing might affect detections and 280 µHz is roughly the Nyquist frequency of TESS. The *TESS*-SCVZ CMD has a number of important features, such as a prominent red clump (RC) at  $M_{K_S} \approx -1.5$ , a clear red giant branch (RGB) extending over the full range in  $M_{K_S}$  and the asymptotic giant branch bump at  $M_{K_S} \approx -3$ . Each pipeline makes asteroseismic detections across all of these evolutionary stages.

initial estimate (or prior) on stellar mass. Assuming the simple scaling for the oscillation amplitudes as in Chaplin et al. (2011), mass has a limited impact on the detectability of the oscillations. More complex relationships have now been demonstrated in the literature, (e.g. Samadi et al. 2012; Corsaro et al. 2013; Yu et al. 2018), however since the uncertainty on the predicted  $v_{max}$  is likely already large, we adopt the simpler relationship. We use the PARSEC stellar evolution models (Bressan et al. 2012; Marigo et al. 2017) to determine a prior on the stellar mass by comparison with the 2MASS photometry of each star, as well as computing the yield assuming a fixed mass  $M = 1.1 \text{ M}_{\odot}$ . Since these give similar results, we focus below on the statistics based on the mass prior from PARSEC. Importantly, we also model the effects of dilution or 'wash-out' of the asteroseismic signal of the target star by the oscillations of other stars in the photometric aperture following Campante et al. (2016) (This may also be referred to as 'crowding'). We implement this by finding the ratio of flux of all stars inside each target aperture in Gaia DR2 (down to G = 17) to that of the target star. This ratio, D, is then factored into the expressions for total mean mode power and granulation power when estimating the probability of detection (see equations 5 and 12 in Campante et al. 2016).

We define all detection yields as the fraction of stars out of the 8,249 with *Gaia*-based luminosity estimates which had successful detections of  $v_{max}$  and  $\Delta v$  that were confirmed using photometric luminosities. The fiducial model, accounting for the time-series

<sup>4</sup> https://github.com/jmackereth/asteroestimate



**Figure 3.** The detection yield  $f_{detect}$  as a function of the number of sectors  $N_{sectors}$ , absolute *H*-band magnitude  $M_H$  and effective temperature  $T_{eff}$  from SkyMapper. The coloured histograms show  $f_{detect}$  for each pipeline considered, based on photometrically confirmed detections (see Appendix C). The dotted curves show the model yield (as in Figure 2) assuming a stellar mass  $M = 1.1 \text{ M}_{\odot}$  not including (blue) and including (orange) dilution effects (see text), respectively. The solid black curve shows the predicted yield (including dilution) when intrinsic stellar parameters are sampled by comparing the 2MASS photometry with the PARSEC isochrones. The observed detection yield has a relatively low dependence on the number of sectors, but has a clear peak in  $M_H$  and  $T_{eff}$ , where the oscillation modes are detected best.

length and dilution effects predicts an average detection yield of  $\sim 46\%$ . The overall detection yield over the seismic pipelines is  $\sim 36\%$  ( $\sim 2,890$  stars) across the whole sample. However, the mean observed yields are  $\sim 50\%$  for stars with the full 13 sectors of data. We find that there are 6388 stars (41% of the entire 15,405 star parent sample, and 1693 of which are in the 'true' CVZ) that had detections in common, but not necessarily consistent, between all three pipelines. Below, we define a 'gold' sample from the subset of these stars, for which the global parameters were highly consistent.

Figure 2 demonstrates the colour-magnitude diagram (CMD) of the *TESS*-SCVZ bright giant sample. The coloured contours demonstrate the regions that contain approximately 90% of the stars with detections in each pipeline. The black dashed line shows the region containing 90% of the stars that had a high detection probability in our fiducial detection model with dilution. Each pipeline covers a region of the CMD that contains a number of interesting features, such as the red clump, giant branch and asymptotic giant branch bump (these are discussed more specifically in section 3).

Figure 3 shows the yield  $f_{detect}$  for each pipeline (coloured histograms) as a function of number of sectors observed  $N_{\text{sectors}}$ , absolute *H*-band magnitude  $M_H$  and effective temperature  $T_{\rm eff}$  (from SkyMapper). The coloured dashed curves show the expected yield from the detection models with and without dilution. The solid black curve shows the predicted yield for the fiducial model based on the PARSEC mass prior including dilution. While the details and performance of the individual pipelines are discussed in their respective papers, it is worth noting that they generally agree in terms of where the greatest yields can be achieved. It is clear that there is a range in  $M_H$  and  $T_{\text{eff}}$  where the global seismic parameters can be readily measured, between  $-4 \leq M_H \leq 0$  and  $4000 \leq T_{\text{eff}} \leq 5000$ , consistent with the expected range from the model. Not allowing for dilution leads to an additional ~ 20% predicted yield in all cases, suggesting that the large pixel size of TESS negatively affects seismic yields, as expected. Evidently, from Figures 2 and 3, the pipelines perform best for less evolved giants, which are fainter and hotter. These stars were more abundant in the Kepler sample, where these pipelines have been well-tested. The effect of the highpass filtering applied to the light curves likely also biases our analysis against the brighter giants which are predicted to have detectable oscillations.

Small differences due to population effects are evident between the PARSEC prior and the fixed mass yield models. Higher mass targets are slightly under-detected relative to lower mass stars (this will change depending on the adopted scaling relation for  $A_{max}$ ). Proper modelling of these effects will be of particular importance, for example, when trying to ascertain the Galactic star formation history based on asteroseismic samples from *TESS*, as it will impose a bias on the derived seismic age distribution against younger (and therefore more massive) targets. However, the simpler target selection of this sample makes this inherently possible, as the simple selection in colour-magnitude space is invertible using stellar population models.

We make a brief check of the internal consistency between the measurements of the global seismic parameters of the pipelines considered here in Figure 4. We compare the results from the COR and A2Z pipelines to those from BHM to assess which, if any, pipelines are internally consistent. The summary statistics are shown in the upper left of each panel. The left panels reveal that in general the pipelines agree on  $v_{max}$  at a level of 3 to 4 percent, with no significant offsets from the global mean. The average consistency in  $\Delta v$  is smaller between COR and BHM, at a level of ~ 2 percent, but is hampered between A2Z and BHM due to a set of Red Clump giants whose  $\Delta v$  measures are significantly different. We find similar inconsistencies between COR and A2Z. There is, however, still a core set of stars for which this parameter is consistent at the < 2 percent level (indicated by the dashed grey lines in each panel). It is conceivable that  $\Delta v$  measures should suffer for shorter time series data. However, we find that the stars with  $N_{\text{sectors}} < 3$  are consistent at a similar level to those with  $N_{\text{sectors}} = 13$ . This likely indicates some issue in definition of  $\Delta v$  between pipelines, or some systematic issue in our TESS light curves that is affecting this measurement in the A2Z pipeline. For example, with few detectable orders, the definition of  $\Delta v$  as the mean or median frequency spacing or some other weighting of these separations becomes important. Pipelines tend to differ in this regard and so may return significantly different results. The effect of this is clearly seen as larger inconsistency at low  $\langle \Delta v \rangle$ , and indeed in  $v_{max}$ , in Figure 4. Extending the time series with data from the extended TESS mission will improve the data in this regard, but there is almost certainly finetuning that still needs to be applied to achieve the best results from all pipelines.



**Figure 4.** Internal consistency between pipelines. Left panels compare the  $\nu_{max}$  returned by the COR and A2Z pipelines to the measurement from the BHM pipeline. Right panels show the same for  $\Delta \nu$ . Only stars for which results were returned in both relevant pipelines are shown. We highlight stars that have the full 13 sectors of data from *TESS*. The mean and standard deviation of the marginalised distributions are shown in the top left of each panel. In general, any differences are on the few percent level.

To determine a sample of stars where all pipelines return consistent parameters, we compute the global mean of parameter measurements in cases where parameters were returned from all three pipelines. There are 5,574 stars (1521 in the 'true' CVZ) for which the parameter measurements from all pipelines were consistent with the global mean within their combined uncertainty. This subset is somewhat reduced from the 6,388 stars with detections in all pipelines. Much of this is driven by inconsistencies in  $\Delta v$  noted above. The relatively large number of stars entering this 'gold' sample indicates that the pipelines are estimating uncertainties well. As an example, the median combined uncertainty on  $v_{max}$  is 1.73  $\mu$ Hz or ~ 5 percent. For  $\Delta v$  the median uncertainty is 0.12  $\mu$ Hz, or ~ 3 percent. Determinations of  $\Delta v$  from individual pipelines generally have lower uncertainties than the mean values. For the remainder of the paper, we choose to use the BHM values as standard in order to demonstrate the prospects for TESS, since these were the results with the greatest consistency with the COR pipeline. The selection of a single pipeline does not significantly affect the results of the following sections, but BHM makes a natural choice since its measured  $\Delta v$  is defined similarly to that derived for the stellar models (Elsworth et al. 2020). Furthermore, in testing, we find that there is little difference (less than ~  $0.3\sigma$ ) between the  $\Delta v$  values returned by BHM and those catalogued by Yu et al. (2018) for stars in the Kepler field. The Yu et al. (2018) results agree very closely with those from individual mode frequencies and so are a good benchmark (Khan et al. 2019). Despite this selection, we still include the global mean values and the seismic gold sample identifier in our published catalogue (see Table ?? in Appendix D), recommending these stars as a benchmark for the TESS-SCVZ, but noting that these early values should be used with certain cautionary steps, also outlined briefly in Appendix D.

#### 3.2.1 Galaxia model

We assess the future potential for seismic samples using TESS data with a simple model of the SCVZ generated using Galaxia (Sharma et al. 2011). Galaxia generates realistic stellar populations with realistic spatial distributions by sampling from a density model fit to Milky Way data and stellar models. For the model, we compute the 2MASS and Gaia photometry using bolometric-corrections. We then compute the detection yield in the model using the procedure above (using the stellar parameters given by Galaxia), extending the sample down to fainter magnitudes to gain an insight into the statistics available for fainter Gmagnitude stars. Again, we include dilution by other sources within the target apertures. We use the parameters provided by the stellar models in Galaxia (which are derived from the PARSEC library: Bressan et al. 2012; Marigo et al. 2017; Rodrigues et al. 2017) to estimate  $v_{\text{max}}$  for each star in the model via the usual asteroseismic scaling relations and use the mass provided as input to asteroestimate.

Figure 5 summarises the statistics from our Galaxia model in comparison with our realised and modelled yields. The top panel demonstrates the range of  $v_{max}$  for which seismic detections are theoretically possible as a function of *G*, compared to those detected by the BHM pipeline (we note that this range is nearly identical for all pipelines). Our model predicts detections down to well below  $v_{max} < 10 \ \mu$ Hz for the  $N_{sectors} > 11$  data. Extending the sample to fainter magnitudes than the currently adopted G = 11 limit (demonstrated by the vertical dashed line) will require better characterisation of these intrinsically low  $v_{max}$  targets. At fainter magnitudes, the observable giants are dominated by intrinsically bright (and therefore low  $v_{max}$ ) upper RGB and AGB stars. For stars with  $N_{\text{sectors}} = 1$  the predicted detectable range of  $\nu_{\text{max}}$  is significantly decreased, owing to the fact that low frequency oscillations are not well sampled by the shorter time series.

The lower two panels of Figure 5 demonstrate the attainable detection yields (middle panel) and absolute sample size (lower panel) predicted by the Galaxia model in our adopted magnitude range, and at fainter magnitudes. The middle panel compares the predicted yield from Galaxia for different  $N_{\text{sectors}}$  (fine dashed lines) with those realised from our pipelines and predicted by the model based on observations. The solid curves show the cumulative fraction of detections as a function of G, indicating the fraction of all possible detections made at each G limit. At faint  $G \ge 9$ , the realised yields agree well with those from Galaxia, suggesting that yield predictions based on the Galaxia model at fainter magnitudes are trustworthy. The yield turns over strongly at G > 11, suggesting this is roughly the limit for detectable giants in TESS. The Galaxia model suggests that there are many detectable brighter giants, however. The absolute cumulative detection counts shown in the lower panel also reflect this. It is likely that least some of these bright stars may be missed in our parent sample due to selection effects in Gaia (Boubert & Everall 2020) and our own imposed limits on parallax SNR, for example. Analyses of bright targets in Kepler have shown that such stars require specialised reduction (White et al. 2017), and this is likely also true for TESS.

This simple model demonstrates that somewhat increased seismic sample sizes are attainable at fainter magnitude limits, albeit at the cost to the detection 'hit-rate'. Based on our observed yields, we predict that there are likely a few hundred more seismically detectable giants in the SCVZ, particularly at brighter *G*. Assuming the NCVZ has similar statistics, across the north and south the potential seismic CVZ giant sample could be as large as  $\sim 10^4$  stars. Based on this model, we predict that seismic detections can be made for  $\sim 3 \times 10^5$  giants across the whole sky (i.e. for  $N_{\text{sectors}} = 1$ , subject to the limits on  $v_{\text{max}}$  outlined above (in good agreement with the expectations of Silva Aguirre et al. 2020).

#### 3.3 Constraints on stellar mass and age

Using PARAM, we make constraints on mass and age for the set of stars with BHM results that had consistent  $v_{max}$  and  $\Delta v$  with the COR and A2Z pipelines, and that had seismic luminosities consistent with those derived from *Gaia* (i.e. numax\_dnu\_consistent = 1 and lum\_flag\_BHM = 1 when using the catalogue presented in Appendix D). The resulting sample has 1,749 stars, although we include PARAM results in the final catalogue for every target that had BHM results and *SkyMapper/TESS*-HERMES parameters which did not meet these criteria (4,453 stars). Additionally, we provide PARAM results for the 351 of the 513 stars with APOGEE spectra that had robust BHM results, using the APOGEE catalogue stellar parameters as constraints.

Since the seismology results are likely to not yet be optimal, we test how the inclusion of *Gaia* luminosity,  $L_{\text{phot.}}$ , as a constraint for PARAM influences the accuracy and precision of our mass and age constraints. The median precision on  $v_{\text{max}}$  and  $\Delta v$ , at a level of 5% and 3%, will not currently provide adequate constraints on mass and age without additional constraints, although individual pipelines report measurements of these parameters at much higher precision. In Figure 6 we show the distribution of fractional uncertainty in mass and age for the 1,749 star sample described above. These uncertainties are 'internal' in the sense that they assume that the grid of stellar models used in PARAM are correct in an absolute sense. Dashed histograms show uncertainties when  $L_{\text{phot.}}$  is not in-



**Figure 5.** Detection statistics from a Galaxia model of *TESS*-SCVZ giant stars selected using the same photometric cuts as our giants, compared to the realised detection yields (and predictions) of the observed bright giants. The top panel shows the predicted detectable and observed (by the BHM pipeline) range of  $v_{max}$  as a function of *G* and for  $N_{sectors} = 1$  and 11. The middle panel shows the detection yield  $f_{detect}$  (dashed lines) and cumulative fractional detections (solid lines) as a function of *N*<sub>sectors</sub>. The lower panel gives the absolute cumulative number of detections as a function of *G*. We compare the model yields with the observed and predicted yields based on our observational sample, which are shown by the wide dashed lines (coloured as in Figure 2 and 3) in the lower two panels.

cluded as a constraint in PARAM, whereas the solid histograms show the same when  $L_{\text{phot.}}$  is included. The uncertainties are clearly tightened up when luminosity constraints are included. Formally, the median uncertainty on mass decreases from 15% to 8%, and on age from 50% to 26%. Without using  $L_{\text{phot.}}$ , the age uncertainties have a large spread, with many stars exceeding 70% uncertainties, whereas its inclusion reduces 93% of the stars to uncertainties of less than 40%. Clearly, improving precision and accuracy on luminosities with better spectroscopic data, for example, will improve our constraints on mass and age. Furthermore, this demonstrates that the *TESS* seismic results are not yet optimal, and can be improved via refinements of the light curves and analyses of them.

For the remainder of the paper, we focus solely on the results which use  $L_{\text{phot.}}$  as an additional constraint. Furthermore, we include only these results in our final catalogue, as they are likely to be the most robust. We refer to results based on the *SkyMapper/TESS*-HERMES parameters as  $age_{SM}$  and  $M_{SM}$ , and those based on APOGEE spectroscopic constraints as  $age_{APO}$  and  $M_{APO}$ .



Figure 6. Histograms of fractional formal uncertainties on mass (blue) and age (red) from PARAM using *SkyMapper/TESS*-HERMES stellar parameters and BHM seismic results. We compare the effect of including *Gaia* luminosity as a constraint between the dashed (no luminosity) and solid (including luminosity) histograms for age and mass. Inclusion of the *Gaia* luminosity improves the median uncertainties from 15% to 8% in mass, and 50% to 26% in age.

# 3.4 Stellar Astrophysics

The potential for *TESS* to provide accurate asteroseismic parameters for many giants on an all-sky basis has been shown for singlesector 27-day data by Silva Aguirre et al. (2020). The year-long data provided by targets in the CVZ in the North and South allows detections of asteroseismic signal at lower frequencies, making the seismic parameters of brighter (and thus larger radii) giants more readily measurable. Longer time-series also afford higher frequency resolution, which allow features in the spectra from mixed modes and rotational splitting to be measured (e.g. Mosser et al. 2019). Shorter time series make such analyses more difficult (e.g. Campante et al. 2019). In this section, we demonstrate the prospects for new constraints on models of stellar structure and evolution using asteroseismology of giants in the 13 sectors of data in the CVZ.

Figure 7 shows examples of power spectra for stars in the TESS-SCVZ sample at different evolutionary stages. The right panel shows stellar mass M as estimated using the BHM seismic and SkyMapper/TESS-HERMES spectroscopic parameters in PARAM against the absolute  $K_S$ -band magnitude  $M_{K_S}$ , computed using the Gaia DR2 parallaxes. The lines plotted underneath show evolutionary tracks from the PARSEC stellar evolution models (Bressan et al. 2012; Marigo et al. 2017). Each line is coloured by the evolutionary stage as provided in the PARSEC tracks and shaded to reflect the relative time spent by a star at each point, emphasising the phases where an overdensity of stars should be expected. The mass- $M_{K_S}$  distribution of the TESS-SCVZ giants roughly matches the prediction of the PARSEC tracks, with the Red Clump (RC) clearly visible. There is also an overdensity at brighter  $M_{K_s}$  than the RC, which corresponds with the Asymptotic Giant Branch (AGB) phase in the PARSEC tracks. Many of these stars are likely to be in the AGB 'bump'. This feature was originally highlighted in stellar tracks by Caputo et al. (1978), observed in external galaxies by Gallart (1998) and recently characterised in Kepler by Bossini et al. (2015).

The left hand panels of Figure 7 show the power spectra of the stars indicated in the right panel, which were selected as examples of the main evolutionary stages which are represented in the data.

The top panel shows a star with a very low  $v_{\text{max}}$  ( < 12  $\mu$ Hz), at an  $M_{K_S}$  and  $M_G$  value consistent with that of AGBb stars . Oscillation modes are clearly present, but have a more complex structure (since they are further from the asymptotic regime, e.g. Stello et al. 2014). This complexity is evident in modelled oscillations of such stars. The luminosity ratio between the RC and the AGBb is of importance in constraining the size of the C-O core at the end of the core-He burning phase, given its weak dependence on the metallicity and initial helium abundance (e.g. Bono et al. 1995). The TESS-CVZ bright giant sample provides a largely unbiased sample of these early AGB stars for which detailed seismic inference is possible. The target selection of e.g. Kepler was complex and biased against luminous stars (see, e.g. Pinsonneault et al. 2014; Girardi et al. 2015; Sharma et al. 2016), while K2 only measures short time-series and therefore does not provide the necessary frequency resolution (see, e.g. Figure 1 of Stello et al. 2015).

The lower two panels on the left hand side of Figure 7 show spectra of exemplar RC and Red Giant Branch (RGB) stars. Again here, oscillation modes are clearly detected in both stars. RGB and RC stars have been examined in detail in previous asteroseismic samples from e.g. CoRoT, *Kepler* and also in *TESS*. For this reason, our prior knowledge of their mode structure is good, facilitating their automated detection (peak-bagging) using the PBJam<sup>5</sup> code (Nielsen et al. 2020, submitted). The  $\ell = 0$  and  $\ell = 2$  modes are cleanly detected and are shown by the red vertical lines in the inset panels.  $\ell = 1$  modes are visible in between the l = 0, 2 pairs, with clear evidence of mixed pressure and gravity modes visible within each order. While we do not make use of individual mode measurements in our analysis, this demonstrates that such analyses are inherently possible with *TESS*.

We further demonstrate the ability of the TESS-CVZ data to study mixed modes and rotational splitting in red giant stars in Figure 8. We show the power spectrum around  $v_{max}$  for an RC giant identified using methods outlined in Vrard et al. (2016). In the left hand panel, the nearest five radial orders to  $v_{max}$  are shown. The right panel shows the modes at n = 6, 7, 8, and the results of a fit to the  $\ell = 0, 1$  and 2 modes following Mosser et al. (2015, 2018). The solid black line shows the power spectrum based on the full 13 sector data set, whereas the underlying dashed red line shows the same generated based on just 27 days (a single sector) of data. In the left panel, we identify the positions of  $\ell = 0, 2$  modes as fit by PB jam (blue and yellow vertical bands, width indicates 95% confidence interval). The structure between these modes is due to  $\ell = 1$  dipole modes. It is evident in the 13 sector curve that these modes divide into multiple separated peaks, whereas such behaviour is not visible in the single sector data (dashed line). In red giant stars, mixed modes are generated by coupling of pressure and gravity modes, which is related to the density contrast between the core and the convective envelope of the star (e.g. Montalbán et al. 2010; Bedding et al. 2011; Beck et al. 2011; Mosser et al. 2012). The fit to the dipole modes in the right panel shows that not only do we detect mixed modes, but also tentatively detect splitting within these modes due to stellar rotation. The best fit mean rotational splitting of the mixed modes is  $\delta v_{rot} = 50$  nHz, with a similar splitting indicated across multiple orders. It is important to note that this value is just above the threshold of  $\delta v_{rot} \simeq 30$  nHz implied by the frequency resolution. Our detection of rotational splitting in an RC star here is comparable in scale to initial measurements of red giants based on  $\sim$  500 days of *Kepler* data (Beck et al. 2012).

<sup>5</sup> https://github.com/grd349/PBjam



**Figure 7.** *Left:* Examples of the seismic detections made by *TESS* across the evolutionary stages of giants in the CVZ. Clear power excess is seen in the log-log space spectra, and oscillation modes are resolved within these envelopes. The l = 0 and l = 2 modes are shown by the red solid and dashed vertical lines (respectively) in the lower two panels. The top panel shows a candidate AGB bump star, which has a complicated mode structure. *Right:* Mass against absolute  $K_S$  band magnitude  $M_{K_S}$  for CVZ giants with detections in the BHM pipeline (which have a seismic luminosity consistent with that from *Gaia*), compared with a set of solar metallicity isochrones from PARSEC, with the evolutionary stages demonstrated in colour. The Red Clump phase is divided into three stages RC, 2RC, 3RC, which represent the core Helium burning phase of low, intermediate and high mass stars, respectively. Red Clump giants whose state is confirmed using the methods of Vrard et al. (2016) are shown as green scatter points. The histograms demonstrate the marginalised distribution of mass and  $M_{K_S}$  (the full underlying distribution of  $M_{K_S}$  is shown in gray). The positions of the example stars in this space are indicated by large white points, and the  $M_{K_S}$  range at which  $v_{max}$  is equal to 10 and 280  $\mu$ Hz at each mass (for a representative range in  $T_{eff}$ ) is shown by the labeled blue bands.



Figure 8. Example of mixed modes visible in a red clump giant identified using the period spacing method of Vrard et al. (2016). The spectrum around the power envelope is shown on the left, with zoomed sections at each radial order on the right. The  $\ell = 0, 2$  modes (identified with PBJam) are indicated by the blue and yellow bands. At each order, a 'forest' of  $\ell = 1$  modes is clearly visible, split into a number of separated peaks. The power spectrum of the same star based on 1 sector of data is shown by the red dashed line, demonstrating that these modes would not be detected in that data. A fit to the oscillation modes following the methods of Mosser et al. (2015, 2018) is shown by the dashed and solid vertical lines in the right panel. Solid lines show the observed modes, whereas dashed shows the prediction of the asymptotic relation. Blue and yellow bands indicate  $\ell = 0, 2$  modes, as before. Red lines show the positions of the  $\ell = 1$  mixed modes detected in the fit, which are split by stellar rotation at a level of  $\delta v_{rot} = 50$  nHz.



Figure 9. Mass vs the ratio of Carbon and Nitrogen abundances, [C/N], for the 351 *TESS*-CVZ stars with results from PARAM based on APOGEE spectroscopic constraints and BHM seismic results, compared to the same relationship from the study of *Kepler* stars by Miglio et al. (2020) (shown as small black points). The *TESS*-SCVZ points are coloured by the age derived from PARAM, and the median uncertainty on Mass and [C/N] is demonstrated at three characteristic masses by the black error bars. The *TESS*-SCVZ results broadly follow the same trends as those from *Kepler*.

Finally, in Figure 9, we demonstrate that the trend between stellar mass and ratio of the photospheric Carbon and Nitrogen abundances, [C/N], which is readily seen in APOKASC and other data-sets (e.g. Martig et al. 2016; Masseron & Gilmore 2015; Silva Aguirre et al. 2020), is also broadly reproduced by our TESS-SCVZ results. Here, we use the subset of stars in our sample which have APOGEE spectra, that were re-analysed in PARAM with these tighter spectroscopic constraints. We compare with the dataset of (Miglio et al. 2020), which used a very similar analysis to derive stellar mass. The [C/N] has a relationship with mass in giant stars due to the first dredge-up (FDU) of material from the stellar interior as the star evolves away from the main sequence (e.g. Salaris et al. 2015; Lagarde et al. 2017). Burning of Hydrogen by the CN and then CNO cycle while on the main sequence produces Nitrogen in the stellar core. The convective envelope during the FDU reaches deeper into the interior for more massive stars, which increases the surface [C/N] on the RGB. This effect is clearly seen in the TESS-CVZ data.

#### 3.5 Galactic Archaeology

Stellar ages are essential, alongside element abundance information and kinematics, to the understanding of the formation and evolution of our Galaxy. As we have shown, TESS can provide reliable seismic constraints for  $\sim 10^5$  giants in the nearby Milky Way, across the whole sky, and ~  $10^4$  with at least 1 year of data. In combination with spectroscopic constraints and modelling, seismic parameters derived from these light curves will provide these essential age constraints. Seismology and stellar modelling presently provides one of the most precise means by which to determine stellar ages (with success already in TESS e.g. Silva Aguirre et al. 2020), and perform detailed studies of the formation and evolution of the Galaxy (e.g. Miglio et al. 2013; Casagrande et al. 2016; Anders et al. 2017a,b; Silva Aguirre et al. 2018; Miglio et al. 2020; Montalbán et al. 2020). These accurate age constraints then provide ideal training sets for data-driven methods of age estimation which can be applied to even larger data sets (e.g. Mackereth et al. 2019; Das & Sanders 2019; Hasselquist et al. 2019; Ciucă et al. 2020). Here



**Figure 10.** Kinematics of the *TESS*-SCVZ sample with age estimates based on the BHM seismic constraints and *SkyMapper* stellar parameters. The top panel shows the  $v_R - v_T$  plane, and the bottom shows  $v_R - v_z$ . Points show each star from the sample with reliably measured ages, coloured by the age estimate from **PARAM**, plotted in reverse order, such that the youngest stars appear in the foreground. The contours demonstrate the kinematics of the full underlying sample. The commonly discussed velocity substructures in the disc (e.g. the *Hercules* stream/gap feature at  $v_R < 0$  km s<sup>-1</sup>,  $v_T <$ 210 km s<sup>-1</sup>) are visible in the underlying sample, and we indicate this in the top panel by the thick dashed line. The stars for which we have measured ages appear to sample these features well.

we present a prospective look at the Galactic Archaeology potential of *TESS*.

We first show the kinematics of the sample in Figure 10. The coloured points show the radial to tangential velocity  $v_R - v_T$  (top) and radial to vertical velocity  $v_R - v_z$  (bottom) distribution of the sample with robust ages, determined using the BHM seismic constraints and SkyMapper parameters, with the colour corresponding to the median age of the posterior distribution from PARAM. The contours show the same kinematics for the full underlying sample of TESS-CVZ giants. Many of the commonly discussed velocity space substructures at the solar vicinity are visible in the full sample. In particular, the Hercules stream/gap (e.g. Dehnen 1998) is visible in the lower left of the distribution of the top panel. A tentative inspection of stars either side of this gap reveals that those at low  $v_T$  seem to have slightly older ages. Recent studies of moving groups in age space have shown that there may be important constraints on the disk dynamics to be made based on relative ages such as these (Laporte et al. 2020). Furthermore, the TESS-CVZ sample, and larger samples enabled by the use of 1-sector *TESS* data or fainter stars will provide new constraints on the local age-velocity dispersion relation (also recently studied in detail by e.g. Ting & Rix 2018; Mackereth et al. 2019; Miglio et al. 2020). In the bottom panel of Figure 10 the eldest stars clearly have the largest dispersion in  $v_R$  and  $v_z$ .

In Figure 11, we demonstrate how even the limited spatial extent of the TESS-SCVZ sample still 'dynamically' samples a large part of the Galactic disc. Using the kinematic information from Gaia-DR2 shown above, we integrate the present day orbits of each star backwards in galpy's MWPotential2014 axisymmetric, static potential. For stars with age estimates from PARAM (using the BHM pipeline results and SkyMapper parameters), we integrate to that age. For stars with no age estimate, we integrate to 2 Gyr ago, which is the typical age of stars for which ages could be determined. In the left panel of Figure 11, we show the resulting distribution of mean orbital Galactocentric radii R<sub>mean</sub> as compared to the present day radial extent (shown by the vertical black lines). The right panels demonstrate the spatial positions in the Galaxy (in an edge on and face on view) of the sample after the back-integration, in comparison with the approximate present day spatial extent of the sample, shown by the black triangles. It is clear that the stars present in the TESS-SCVZ are members (in a dynamical sense) of a far more widely distributed population. While this is of course true for any local sample or field, it emphatically demonstrates the richness of the seismic data available.

Figure 12 shows the trends between the stellar mass (which is determined more precisely than the age in most cases) and the mean orbital radius  $r_{mean}$  and maximum vertical excursion from the midplane  $z_{max}$ . At increased stellar mass (and therefore younger ages on average), the width of the  $r_{mean}$  distribution decreases markedly, such that the lowest mass stars have orbits whose mean radii cover the largest extent of the disc. This is a clear signal of radial mixing of disc stars, and has been noted in a number of studies (e.g. Casagrande et al. 2011; Frankel et al. 2018, 2019, 2020; Miglio et al. 2020; Sharma et al. 2020). Similarly, at lower mass, stars have a wider distribution in  $z_{max}$ , a clear example of dynamical heating of the disc (e.g. Aumer et al. 2016; Ting & Rix 2018; Mackereth et al. 2019). The measurement of precise ages for nearby stellar samples provides an ideal dataset for testing models of radial mixing and dynamical heating processes.

Further, Figure 13 demonstrates the relationship between age, element abundances and kinematics of the TESS-SCVZ sample with APOGEE DR16 spectra (513 stars). The top panel shows the [Fe/H]-[Mg/Fe] plane (which has been studied extensively in a Galactic Archaeology context, e.g. Haywood et al. 2013; Nidever et al. 2014; Hayden et al. 2015; Queiroz et al. 2020) coloured by the stellar age (based on analysis using the more precise APOGEE DR16 stellar parameters). The high [Mg/Fe] stars which separate from the solar [Mg/Fe] population at [Fe/H]  $\leq 0.2$  are clearly separate in age, and are generally older than  $\sim 10$  Gyr (aside from some notable outliers, see below). The solar [Mg/Fe] population has a wider spread in ages below  $\sim 10$  Gyr, and a relatively clear trend toward younger age with decreasing [Mg/Fe]. These trends are also broadly seen in other studies of the [Fe/H]-[Mg/Fe] plane with stellar ages (or their proxies, e.g. Haywood et al. 2013; Anders et al. 2017a; Hasselquist et al. 2019; Mackereth et al. 2019).

This trend is much clearer in the lower right panel, which shows [Mg/Fe] as a function of age, now coloured by the mean orbital radius for each star. As age increases from ~ 0 Gyr up to ~ 10 Gyr, the mean [Mg/Fe] increases by almost 0.1 dex. Stars older than ~ 10 Gyr have a larger spread in [Mg/Fe] and are those corresponding to the high [Mg/Fe] track in the upper panel. The  $R_{\text{mean}}$  of these stars indicates that they are likely to be members of populations formed in the inner disc of the Galaxy which have eccentric orbits and thus have travelled to the solar radius.

The mean orbital radii also indicate useful information in the lower left panel, showing [Fe/H] as a function of age, again coloured by  $R_{mean}$ . At intermediate age (~ 3 to 8 Gyr) and, to a lesser extent outside of this range, there is a large spread in [Fe/H] at fixed age. Stars with high  $R_{mean}$  tend to be young and have lower [Fe/H]. The most metal rich stars are old and have lower  $R_{mean}$ . This gradient in  $R_{mean}$  across the range in [Fe/H] is to be expected given that the Milky Way disc has a shallow, yet significant, metallicity gradient (e.g. Cheng et al. 2012; Bergemann et al. 2014; Anders et al. 2017b). The lack of a clear relationship between age and [Fe/H] is likely a manifestation of radial migration in the disc, and has been discussed at length in the literature (Sellwood & Binney 2002; Solway et al. 2012; Minchev et al. 2012, 2013; Vera-Ciro et al. 2014; Grand et al. 2015; Frankel et al. 2018, 2020).

Finally, we show the age distributions of our samples in Figure 14. We divide the APOGEE based ages into high and low [Mg/Fe] groups, using the visually determined division shown in the top panel of Figure 13. We estimate the posterior distribution of the observed ages using a Gaussian kernel density estimation applied to 1000 samples from the posterior on each star from PARAM. The SkyMapper and low [Mg/Fe] APOGEE ages have qualitatively similar distributions, suggesting that the SkyMapper sample is dominated by low [Mg/Fe] stars. The high [Mg/Fe] stars have a bimodal age distribution, with a strong peak at  $\sim 10$  Gyr. This peak is consistent with the old age for the high  $[\alpha/Fe]$  disc as shown by a number of studies (e.g. Fuhrmann 2011; Haywood et al. 2013; Silva Aguirre et al. 2018; Miglio et al. 2020). The young peak is likely to be a result of 'over-massive', apparently 'young'  $\alpha$ -rich stars, contaminating the sample (Martig et al. 2015; Chiappini et al. 2015; Jofré et al. 2016; Hekker & Johnson 2019). These stars are outliers to the true age distibution of the high  $\left[\alpha/\text{Fe}\right]$  disc. Evidence collected thus far strongly suggests that these are stars which have undergone some mass transfer with a (now unseen) companion earlier in their lives and thus appear young to asteroseismic methods (see discussion in, e.g. Miglio et al. 2020). Each sample has a long tail extending to high ages driven by the uncertainties on individual ages, which are Gaussian in  $\log_{10}(age)$ , due to the prior adopted in PARAM.

We fit a mixture model for the intrinsic age distribution of the high [Mg/Fe] stars, following the methodology of Miglio et al. (2020). This model accounts for the contamination by 'overmassive' stars, and recovers the intrinsic spread in age of the population (i.e. other than that caused by the age uncertainties). We find results that are consistent with those of Miglio et al. (2020): the mean age of the population is  $\mu = 11.3 \pm 0.8$  Gyr, with an intrinsic spread (defined as the standard deviation in linear age) of  $\delta_{age} = 1.3^{+0.6}_{-0.8}$  Gyr. The best fit model and the  $1\sigma$  uncertainty are shown by the dashed gray line and band in Figure 14. It is clear that the age uncertainties inflate the distribution considerably, but careful modelling accounting for these uncertainties can recover the underlying age spread. This demonstrates that it will still be possible to make important inferences of, for example, the Galactic star formation history using TESS ages, despite the relatively lower asteroseismic precision (relative to, e.g. Kepler) afforded by the data.

Finally, we note that our mixture model finds a contamination of the high [Mg/Fe] stars by 'over-massive' stars at a level of  $15^{+11}_{-7}$ %. This contamination is a little higher but not inconsistent above the  $1\sigma$  level, than the results of Miglio et al. (2020). It



Figure 11. The spatial extent of the *TESS*-SCVZ sample compared with the extent which is 'dynamically' sampled by the data. The histogram on the left compares the extent in Galactocentric *R* today (blue shaded region) with the distribution of mean orbital radii  $R_{mean}$  in the sample (blue histogram). The right panels show the spatial distribution in Galactocentric Cartesian coordinates when the sample is integrated backwards to its apparent age (coloured points) or 2 Gyr for stars with no age estimates (small black points) in an axisymmetric potential. The approximate extent today of the SCVZ sample is shown by the black triangles.

is likely that the differences in selection between these two works likely brings about some population bias which may affect these numbers. Future studies which aim to determine the origin and nature of these 'over-massive' stars will need to account for these biases.

## 4 SUMMARY & CONCLUSIONS

We have demonstrated the strong potential for Galactic archaeology and stellar astrophysics and asteroseismic quality of year-long photometry from the *TESS*-CVZ. Studying a sample of 15, 405 giants in- and outside the CVZ, we demonstrate that currently achieved seismic yields are comparable or better to those estimated using a model of detection probability in *TESS* and produce precise stellar ages, masses and radii when combined with spectroscopic constraints. Power spectra derived from the time series data provide clear detections of oscillation modes in stars in a large range of evolutionary states, providing great potential for new constraints on stellar evolution models. To summarise our findings:

• Systematics: A number of systematics are evident in the light curves that we generate based on the *TESS* FFI, which appear worsened in the 1 year data. More detailed correction of these will be required to ascertain the best possible seismic data. It is likely that many such issues can be resolved with some extra treatment of our light curves.

• Seismic detection yields: We find that the realised detection yields from the *TESS*-CVZ compare well with a simple model for the detection probability, but only after accounting for dilution effects. After confirming seismic detections using luminosities derived with 2MASS and *Gaia* for 8,249 stars, we find an average detection yield of ~ 36% (2,890 stars), which increases to ~ 50% when stars with a year of data are considered. We presently suffer from issues in procuring seismic parameters for brighter stars with  $v_{max} < 10 \,\mu$ Hz, which likely will require specifically tuned analysis methods.

• Constraints on stellar mass and age: we produce mass and age constraints for 1,749 stars, based on *SkyMapper/TESS*-HERMES stellar parameters and BHM seismic parameters using the PARAM Bayesian parameter estimation code. By comparing the uncertainties on mass and age when *Gaia* luminosities are used as constraints or not, we show that without refining the current seismic parameter measurmements, an external luminosity constraint is required to achieve adequate precision (i.e. less than 10% in mass and 30% in age) on these parameters.

• Seismology across the Hertzsprung-Russell diagram: The *TESS*-CVZ data provides good power spectral resolution even for relatively low  $v_{max}$  stars. We show that stars on the AGB bump are



**Figure 12.** The stellar mass as estimated using PARAM applied to the BHM pipeline and *SkyMapper* parameters, against the mean orbital radius  $r_{mean}$  and the maximum vertical excursion above the plane  $z_{max}$ . The colour of the points is determined by the [Fe/H] from *SkyMapper*. It is clear that the lowest mass (and therefore oldest, on average) stars are those whose orbits cover the greatest radial and vertical extents. There is a clear relationship with [Fe/H], such that at higher mass (and thus younger ages), stars are generally more metal rich.

clearly detected in our sample, and the detection of mixed modes and, tentatively, rotational splitting is possible in RC stars with 12 sectors of data. Importantly, target selection effects are more simply accounted for in the *TESS*-FFI samples than in, for example, *Kepler*. We demonstrate that our data compare well with *Kepler* data analysed in similar ways by showing

• Galactic archaeology in the Milky Way disc: The *TESS*-SCVZ sample provides a good sampling of velocity space in the solar vicinity. Trends between stellar mass (and therefore age) and the mean radii and maximum vertical excursions of stellar orbits are clearly visible. By integrating the orbits of stars in our sample, we demonstrate that the data from the CVZ, although limited in spatial extent, 'dynamically' samples a large section of the Milky Way disc with  $5 \leq R \leq 10$  kpc. The age precision afforded by *TESS*, in combination with high resolution spectroscopic data from APOGEE, is enough to distinguish clear differences in age between the high and low [Mg/Fe] disc stars and will be of great utility in properly reconstructing the star formation history of the disc.

In particular, this paper has demonstrated the great importance of spectroscopic follow up for giants in the *TESS*-CVZs. We predict that seismic samples of the order of a few 10<sup>4</sup> giants could be attainable in the CVZs, but age and mass estimates will only be readily available – and sufficiently precise – for stars which also have spectroscopic information. Such spectroscopic data will likely become available from future survey data (e.g. GALAH: Martell et al. 2017 SDSS-V: Kollmeier et al. 2019), but high resolution, high SNR

samples may be of great utility to the community as calibration data.

Careful modelling of large samples of asteroseismic data will afford detailed insights into the formation and evolution in the disc. Furthermore, it is likely possible to further pin down the precision on these stellar ages, using novel analysis techniques based on machine learning (Blancato et al. 2020; Hon et al. 2018; Ness et al. 2018) or more detailed modelling (and fitting) of the power spectra (e.g. Rendle et al. 2019; Montalbán et al. 2020). In addition to this, it is foreseeable that samples from the CVZs will be useful as training data for future data-driven analyses, providing time-series with consistent noise statistics but longer baselines than the whole-sky *TESS* data.

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**Figure 13.** [Mg/Fe], [Fe/H] and age for the 351 *TESS*-CVZ bright giants which have detailed abundances from APOGEE-DR16 and results from PARAM based on the BHM seismic parameters. The upper panel shows the [Mg/Fe]-[Fe/H] plane coloured by stellar age. The dashed line indicates the visually defined separation which we make between high and low [ $\alpha$ /Fe] stars. The lower panels show each of these abundance ratios as a function of stellar age, and colour indicates there the mean orbital radius  $R_{mean}$  of each star. There is a clear dichotomy in age between the old, high [Mg/Fe] stars and the younger, low [Mg/Fe] stars. Similarly, the older populations have markedly lower mean radii and are on excursions from the inner regions of the disc.



**Figure 14.** The posterior distributions of observed ages for high and low [Mg/Fe] stars in common with APOGEE (shown by the red and blue curves, respectively), and the full sample in common with *SkyMapper* (in gray). We estimate the posterior using a Gaussian kernel density estimation applied to samples from the individual age posteriors from PARAM. The mixture model for the intrinsic age distribution of high [Mg/Fe] stars and its  $1\sigma$  uncertainty is shown by the gray dashed line and band. Despite the relatively large age uncertainties, the mixture model recovers the intrinsic age distribution for high [Mg/Fe] stars found by previous works.

ico State University, New York University, University of Notre Dame, Observatário Nacional / MCTI, The Ohio State University, Pennsylvania State University, Shanghai Astronomical Observatory, United Kingdom Participation Group, Universidad Nacional Autónoma de México, University of Arizona, University of Colorado Boulder, University of Oxford, University of Portsmouth, University of Utah, University of Virginia, University of Washington, University of Wisconsin, Vanderbilt University, and Yale University.

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# DATA AVAILABILITY

The processed data underlying this article are available in the article and in its online supplementary material. The raw data (e.g. unprocessed light curves, original data tables) can be made available on reasonable request to the corresponding author.

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# APPENDIX A: SURFACE GRAVITY CONSTRAINTS FOR STARS WITH MISSING DATA

For the best possible constraints on stellar mass and age using a method such as PARAM, we require as many constraints on other fundamental stellar parameters as possible. At present, the TESS-SCVZ data are lacking in publicly available spectroscopic follow

up, and so these stellar parameters must be gathered by alternative means. As described above, we use a combination of data from *SkyMapper*, *TESS*-HERMES, and APOGEE. There are a number of stars for which an estimate of  $\log(g)$  is not available from *TESS*-HERMES. Here we exploit the fact that there is a correlation between  $T_{\text{eff}}$  and luminosity *L*, which in turn correlates with *R* and thus the surface gravity  $\log(g)$  with some dependence on [Fe/H], to constrain a prior on  $\log(g)$  for stars which have  $T_{\text{eff}}$  and [Fe/H].

We use a simple method to infer  $\log(g)$  for those stars which only had photometric  $T_{\text{eff}}$  and [Fe/H] from *SkyMapper*. Using the 1186 stars in our sample for which spectroscopic  $\log(g)$  was available from *TESS*-HERMES, we construct a Gaussian KDE of  $\log(g)$ ,  $T_{\text{eff}}$  and [Fe/H] space, adopting a kernel with a bandwidth determined via Scott's rule, as implemented in scipy. The resulting KDE is smooth in all three parameters when marginalising over the range of the other parameters, suggesting it provides a fair representation of the prior information on the  $\log(g)$  distribution. By combining the prior information on  $T_{\text{eff}}$  and [Fe/H] for each star (assuming Gaussian uncertainties) with this KDE, we construct the joint posterior probability for all three parameters:

$$\ln p(\log(g), T_{\text{eff}}, [\text{Fe}/\text{H}]) = \ln p(\text{KDE}(\log(g), T_{\text{eff}}, [\text{Fe}/\text{H}])) + \ln p(T_{\text{eff}}) + \ln p([\text{Fe}/\text{H}]), \quad (A1)$$

where  $KDE(log(g), T_{eff}, [Fe/H])$  is the density of the KDE at a given set of parameters, and  $p(T_{eff})$ , p([Fe/H]) are the prior information on  $T_{\text{eff}}$  and [Fe/H] from SkyMapper. For each star with missing log(g), we use rejection sampling to take samples of this posterior within the range of parameters represented in the full data set. We verify that this procedure gives a reliable constraint on log(g) by making an inference of the parameter for the set of stars with TESS-HERMES log(g) constraints, and find that the SkyMapper prior-based log(g) constraint is within  $3\sigma$  of the TESS-HERMES measurement for all 1186 stars, and within  $1\sigma$  for ~ 93% of the sample. This suggests that this inference is reliable for the rest of the dataset, and the resulting uncertainty on the log(g) constraint is realistic and will hence be propagated into our inference of luminosity, mass, age and radii consistently. Figure A1 shows the comparison between our inferred log(g) and that from *TESS*-HERMES. The median uncertainty on the inferred log(g) is 0.3, compared to 0.1 for the TESS-HERMES measurements.

#### APPENDIX B: GAIA PARALLAX ZERO-POINT OFFSET

Since this sample represents an extension to brighter magnitudes of the set of stars with asteroseismic constraints, in a different region of the sky to previously available data (e.g. *Kepler*), it is appropriate to check if and how the derived parallax zero-point offset may change. While this is not the focus of this work and will likely form the basis of future, more detailed, studies based on *TESS* data, we make a simplified assessment of this offset here. Current assessments of the parallax zero-point offset in *Gaia* DR2 yield values of  $30 \leq \Delta \omega \leq 60 \ \mu$ as (e.g. Lindegren et al. 2018; Schönrich et al. 2019; Khan et al. 2019; Hall et al. 2019; Leung & Bovy 2019; Zinn et al. 2019; Chan & Bovy 2020). Furthermore, it has been widely shown that the zero-point is multivariate as a function of position on the sky (e.g. Lindegren et al. 2018; Chan & Bovy 2020), and stellar parameters (e.g. Zinn et al. 2019; Khan et al. 2019).

Here, we make a simple assessment of the zero-point offset for the *TESS*-SCVZ sample only as a function of the apparent  $K_S$ band magnitude. We take the raw *Gaia* DR2 parallax and its associated uncertainty, and derive a 'seismic' parallax by transforming



**Figure A1.** Comparison of  $\log(g)$  from *TESS*-HERMES with that inferred using the *TESS*-HERMES and *SkyMapper* data as prior information. The top panel shows the density distribution of samples from the posterior. when the *TESS*-HERMES  $\log g$  is used, and when the  $\log(g)$  is inferred from the prior. The bottom panel compares the difference between the inferred and measured  $\log(g)$ , normalised by the combined uncertainty  $\sigma_{c}$ . ~ 93% of the inferences of  $\log(g)$  fall within  $1\sigma$  of the measured values, although the uncertainty on the inferred  $\log(g)$  is a factor of 3 greater than those measured by *TESS*-HERMES.

the PARAM  $M_{bol}$  values, estimated using the BHM seismic parameters and the *SkyMapper* stellar parameters, using the bolometric corrections derived for the sample based also on these parameters. We use a separate run of PARAM which did not use the *Gaia* derived luminosity as a constraint such that the luminosity is directly predicted by the seismic and stellar parameters. We then sample the resultant posterior on  $\Delta \varpi = \varpi_{PARAM} - \varpi_{Gaia}$  and  $K_S$  for each star and use the 0.16, 0.5 and 0.84 quartiles as input to our fitting procedure. We use the likelihood function for a linear fit with two dimensional uncertainties (assuming that the uncertainty on  $\Delta \varpi$  and  $K_S$  are uncorrelated) given in equation (32) of Hogg et al. (2010), and sample the posterior distribution of the parameters describing a linear relationship between  $\Delta \varpi$  and  $K_S$  using emcee (Foreman-Mackey et al. 2013).

The resulting fit and posterior samples compared to the data are shown in Figure B1. The data are shown as a two-dimensional histogram of the samples from the posteriors on  $\Delta \varpi$  and  $K_S$ , to give a sense of the large uncertainties on  $\Delta \varpi$ . Despite these large uncertainties, an offset of the mean  $\Delta \varpi$  from 0 is clear. We show offsets of 30 and 50  $\mu$ as as dotted and dashed lines respectively, as a guide to how our derived offset compares with those from the literature. Our best fit model is consistent with being flat as a function of  $K_S$ , with a zero-point offset of ~ 30  $\mu$ as, such that  $\Delta \varpi = (-5 \pm 6)(K_S - 8.) + (30 \pm 3) \mu$ as. This offset is somewhat smaller than many derived using currently available asteroseismic samples (e.g. Hall et al. 2019; Khan et al. 2019; Zinn et al. 2019). This may be a genuine population effect, due to the fact that this



**Figure B1.** The *Gaia* DR2 parallax zero-point offset as a function of  $K_S$  magnitude, as measured by comparing the observed *Gaia* parallax values with those derived by measuring stellar luminosities using the BHM seismic results and PARAM (removing the constraint based on the *Gaia* luminosity). The 2D histogram shows the density of samples from the posteriors on magnitude and parallaxes, assuming Gaussian uncertainties. The dotted and dashed lines demonstrate the levels of common values for the zeropoint offset measured using various techniques. Our best fit model is shown by the solid gray line, and MCMC samples of the posterior likelihood function of the parameters of the fit given the data is shown by the individual black lines. The best fit model gives a dependency of the offset on  $K_S$  of  $\Delta \varpi = (-5 \pm 6)(K_S - 8.) + (30 \pm 3) \mu as$ .

sample is somewhat closer and thus brighter than the *Kepler* sample. This may also reflect noted variations as a function of position on the sky. Future studies of the *TESS* data will likely narrow down this estimation and trends with these parameters.

# APPENDIX C: COMPARING PHOTOMETRIC AND ASTEROSEISMIC LUMINOSITIES

Figure C1 shows the full comparison between  $L_{\text{phot.}}$  and  $L_{\text{seis.}}$  for each of the pipelines considered. We normalise the difference between  $L_{\text{phot.}}$  and  $L_{\text{seis.}}$  by the combined uncertainty on photometric and seismic luminosities  $\sigma_c$ . In this way, a difference of e.g.  $3\sigma_c$ indicates the two measurements are consistent to  $3\sigma$ . The uncertainty on  $L_{\text{seis.}}$  is considerably higher than that on  $L_{\text{phot.}}$  in many cases, which can lead to small values of this difference. However, since this indicates the uncertainties are well estimated, we allow these into our sample. The horizontal lines in each figure show the  $\pm 3\sigma_c$  limit. For each pipeline, we colour the points by  $\nu_{\text{max}}$  and show (as larger points) the stars for which each pipeline returned a  $\nu_{\text{max}}$  close to the diurnal frequency ( $\nu_{\text{max}} = 11.57 \pm 0.1$ ). This will allow us to assess whether the appearance of these detections is real or due to some systematic in the *TESS* photometry.

Inspection of Figure C1 reveals that there are a considerable number of targets across all three pipelines for which  $L_{\text{seis.}}$  is not consistent with  $L_{\text{phot.}}$  (within  $3\sigma_c$ ). In each pipeline, a cloud of 'high'  $v_{\text{max}} \gtrsim 10^2$  detections is visible such that  $L_{\text{seis.}}$  underestimated by  $\simeq 10\sigma_c$ . This means that many intrinsically bright targets have been misidentified by the seismic analysis as high  $v_{\text{max}}$ and therefore low luminosity stars. Visual inspection of the power spectra of a few of these targets shows that it appears that there is genuine power excess at low v as expected from their luminosity. However, a number of features are apparent in the noisier, high v



Figure C1. Comparison between photometrically and seismically derived luminosities. The seismic luminosities  $L_{seis.}$  are estimated using the scaling relations applied to the seismic parameters determined by the BHM, COR and A2Z pipelines, from left to right. The vertical axes give the difference between photometric and seismic luminosity, normalised by the combined uncertainty  $\sigma_c$ . The dashed horizontal lines demonstrate the range at which results are consistent within  $3\sigma_c$ . The majority of stars have consistent luminosities in all three pipelines, but each have clear cases of false positive detections. We highlight stars with  $v_{max}$  near to the diurnal frequency (11.57µHz as larger points, demonstrating that most detections at this frequency appear to be true positives, and not due to systematic effects in our light curves.

part of the power spectrum. This likely indicates some fine-tuning of analysis methods may be necessary for *TESS* power spectra.

Furthermore, it appears that there are a number of genuine and photometrically consistent detections with  $v_{max} \simeq 11.57 \mu$  Hz, suggesting that systematics at this frequency are not as problematic as may be expected, given the scattered light present in many of the *TESS* observations. This also suggests that an apparent 'bump' in the  $v_{max}$  distribution at roughly this frequency may be a real feature.

# APPENDIX D: CATALOGUE OF SEISMIC, PHOTOMETRIC, SPECTROSCOPIC AND KINEMATIC PROPERTIES FOR *TESS*-SCVZ GIANTS

We provide all data necessary for the reproduction of the analyses presented here in a catalogue of the compiled seismic, photometric, spectroscopic and kinematic properties for the 15405 stars in the *TESS*-SCVZ bright red giant sample. The columns included in the data table are described in **??**. All relevant columns described in **??** have associated uncertainties, which are adjacent to those columns in the table. The catalogue reproduces data produced by the *Gaia* (Gaia Collaboration et al. 2018), 2MASS (Skrutskie et al. 2006), *TESS*-HERMES (Sharma et al. 2018), *SkyMapper* (Onken et al. 2019) and APOGEE (Majewski et al. 2017) surveys, and includes orbital parameters estimated as described in section 2.

Since we include all the possible data in the catalogue (i.e. we do not remove stars which we flagged as bad in any way), we recommend that users take care to apply the appropriate selection to any data that is used. For example, we recommend that when using PARAM results, the sample is limited to only those stars with stellar radii measured to be less than  $12R_{\odot}$  (as recommended by Miglio et al. 2020) and those with the appropriate luminosity flag indicating that the seismic parameters are robust relative to the Gaia luminosity. Furthermore, since the internal consistency is not optimal in this first set of data, we recommend that the mean  $v_{max}$  and  $\Delta v$ values are avoided in most cases, as these can represent large deviations from the true values in some cases. Best practice might be to use a set of results from a single pipeline, restricting the sample to only those stars where consistent detections were made across all three pipelines (i.e. numax\_dnu\_consistent = 1), and where the relevant luminosity consistency flag is on (i.e. lum\_flag\_XXX = 1, where XXX is the relevant pipeline identifier). In the case of the BHM results, this provides a sample of 1,749 stars which likely have the most robust data provided by that pipeline.

As an additional way to assess the data quality for individual targets, we include an estimate of the goodness of fit in PARAM through the  $\chi^2$  of the fit for those stars which returned parameter values. This value is computed by comparing the input constraints with those predicted by the best fit model. In this way, a star which is not well represented by the grid of stellar models employed by PARAM will have a high  $\chi^2$ . We reccommend that users check samples for high values of this parameter, especially when using small numbers of stars. Any  $\chi^2$  well above ~ 5 can be considered a poor fit. In the catalogue, these numbers are found under CHI2<sub>g</sub> of<sub>P</sub>ARAM<sub>B</sub>HMand

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 <sup>1</sup>School of Astronomy and Astrophysics, University of Birmingham, Edgbaston, Birmimgham, B15 2TT, UK
 <sup>2</sup> Canadian Institute for Theoretical Astrophysics, University of Toronto, 60 St. George Street, Toronto, ON, M5S 3H8, Canada
 <sup>3</sup> Dunlap Institute for Astronomy and Astrophysics, University of Toronto, 50 St. George Street, Toronto, ON M5S 3H4, Canada
 <sup>4</sup>LESIA, Observatoire de Paris, Université PSL, CNRS, Sorbonne Univer-

sité, Université de Paris, 5 place Jules Janssen, 92195 Meudon, France

<sup>5</sup>Instituto de Astrofísica de Canarias, La Laguna, Tenerife, Spain

<sup>6</sup>Dpto. de Astrofísica, Universidad de La Laguna, La Laguna, Tenerife, Spain

<sup>7</sup>IRFU, CEA, Université Paris-Saclay, F-91191 Gif-sur-Yvette, France <sup>8</sup>AIM, CEA, CNRS, Université Paris-Saclay, Université Paris Diderot,

Sorbonne Paris Cité, F-91191 Gif-sur-Yvette, France

<sup>9</sup>Aix Marseille Univ, CNRS, CNES, LAM, Marseille, France

<sup>10</sup>Istituto Nazionale Astrofisica di Padova - Osservatorio Astronomico di Padova, Vicolo dell'Osservatorio 5, IT-35122, Padova, Italy

<sup>11</sup>Dept. of Astronomy, The Ohio State University, 140 W. 18th Ave., Columbus, OH 43210, USA

<sup>12</sup>Department of Astronomy, Yale University, New Haven, CT, 06520, USA
 <sup>13</sup>Department of Astrophysical Sciences, Princeton University, 4 Ivy Lane,

Princeton, NJ 08544

<sup>14</sup>The Observatories of the Carnegie Institution for Science, 813 Santa Barbara St., Pasadena, CA 91101

<sup>15</sup>Institut für Physik, Universität Graz, Universitätsplatz 5/II, 8020 Graz

<sup>16</sup>Max-Planck Institut für Astronomie, Königstuhl 17, 69117 Heidelberg, Germany

<sup>17</sup>Instituto de Astrofísica e Ciências do Espaço, Universidade do Porto, Rua das Estrelas, 4150-762 Porto, Portugal

<sup>18</sup>Research School of Astronomy and Astrophysics, Mount Stromlo Observatory, The Australian National University, ACT 2611, Australia

<sup>19</sup>Departamento de Física e Astronomia, Faculdade de Ciências da Universidade do Porto, Rua do Campo Alegre, s/n, 4169-007 Porto, Portugal

<sup>20</sup>Leibniz-Institut für Astrophysik Potsdam (AIP), An der Sternwarte 16, 14482 Potsdam, Germany

<sup>21</sup>Department of Astronomy, The Ohio State University, Columbus, OH 43210, USA

<sup>22</sup>Institute of Space Sciences (ICE, CSIC), Carrer de Can Magrans S/N, E-08193, Bellaterra, Spain

<sup>23</sup>Institut d'Estudis Espacials de Cataluna (IEEC), Carrer Gran Capita 2, E-08034, Barcelona, Spain

<sup>24</sup>Stellar Astrophysics Centre, Department of Physics and Astronomy, Aarhus University, Ny Munkegade 120, DK-8000 Aarhus C, Denmark

 <sup>25</sup>School of Physics, University of New South Wales, NSW 2052, Australia
 <sup>26</sup>Institute for Astronomy, University of Hawai'i, 2680 Woodlawn Drive, Honolulu, Hawaii 96822, USA

<sup>27</sup>Carnegie Earth and Planet Laboratory, 5241 Broad Branch Road, N.W., Washington, DC 20015

<sup>28</sup>The Observatories of the Carnegie Institution for Science, 813 Santa Barbara St., Pasadena, CA 91101

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